

MEAN.

Measure of central tendency i.e. average gives the whereabouts of some central value of a series, around which all other observations are dispersed.

Various types of central tendency may be kept under two major heads.

① Mathematical average and

② Averages of position.

① Mathematical average :- Averages represented purely in mathematical value is known as mathematical averages. It is of 3 types: ① Arithmetic mean

② Geometric mean

③ Harmonic mean.

② Averages of position - Mean exhibited by position is called averages of position. It is of two types ① Median & ② Mode.

Arithmetic Mean

Central value or average obtained arithmetically is known as arithmetic mean. It is calculated by summing up all observations of a series & dividing it by the number of observations.

Mean can be calculated from ungrouped (individual series) and grouped (discrete & continuous) data.

① Ungrouped (Individual Series) :- The summation of all values of variables in individual observation divided by the number of observations is the mean of that individual series.

Ex - Suppose each individual observation is $x_1, x_2, x_3, \dots, x_n$
Summation of all observation is $\sum x$. Then $\sum x = x_1 + x_2 + x_3 + \dots + x_n$

Then $\sum X = X_1 + X_2 + X_3 + \dots + X_n$. The number of observation is N . Therefore the arithmetic mean can be calculated by the following formula.

$$\bar{X} = \frac{\sum X}{N} \text{ (Direct method)}$$

$$\bar{X} = w + \frac{(\sum dx')}{N} \text{ (Short cut method).}$$

Where $\bar{X}$ = Mean

$\sum X$ = Summation of all observations

N = Total No. of observations

$\sum dx'$ = Summation of deviations of variables obtained from assumed mean.

Example:- Length of 10 Earthworms in a small garden were measured as follows. Find out the ^{mean} length of Earthworm.

Serial No. of Earthworm : 1, 2, 3, 4, 5, 6, 7, 8, 9, 10.

Lt. of Earthworms in cms : 6, 7, 5, 4, 8, 7, 9, 6, 8, 7.

Calculation by direct method :-

$$\bar{X} = \frac{\sum X}{N}, \bar{X} = \frac{6+7+5+4+8+7+9+6+8+7}{10} = \frac{67}{10} = 6.7 \text{ cm.}$$

Ans.

(b) calculation by short cut method :- Here three columns have been made. First column bear Serial No. of Earthworms. Second column have length of earthworms & third column bear deviation from assumed mean.

Sl. No.	Length in cms X	Deviation from assumed mean (dx)
1	6	$6-8 = -2$
2	7	$7-8 = -1$
3	5	$5-8 = -3$
4	4	$4-8 = -4$
5	8 (w)	$8-8 = 0$
6	7	$7-8 = -1$
7	9	$9-8 = +1$
8	6	$6-8 = -2$
9	8	$8-8 = 0$
10	7	$7-8 = -1$
$N = 10$		$\sum dx' = -13$

Where $w = \text{Assumed mean}$. Here $w = 8$

Formula for short-cut Method to get mean:

$$\bar{X} = w \left(\frac{\sum dx'}{N} \right) = 8 + \frac{-13}{10} = 8 + (-1.3) = 6.7 \text{ cms. Ans.}$$

Grouped data - When data is in frequency distribution.

(A) Discrete Series = Mean in discrete series can be obtained by two methods (i) Direct method & (ii) Short-cut method.

(i) Direct Method :- Summation of variables multiplied by their respective frequencies divided by the total no. of observations is the direct method to obtain mean in discrete series.

$$\bar{X} = \frac{f_1 x_1 + f_2 x_2 + f_3 x_3 + \dots + f_n x_n}{f_1 + f_2 + f_3 + \dots + f_n}$$

$$\bar{X} = \frac{\sum fx}{\sum f} \quad (\text{Direct method})$$

Here $x_1, x_2, x_3, \dots, x_n$ are observations & their respective frequencies are $f_1, f_2, f_3, \dots, f_n$. Summation of observations multiplied by their respective frequencies is $\sum fx$. Then

$$\sum fx = f_1 x_1 + f_2 x_2 + f_3 x_3 + \dots + f_n x_n$$

$$\text{Length of fish} = 5, 15, 25, 35, 45, 55, 65, 75$$

$$\text{Frequency} = 3, 11, 7, 4, 10, 5, 7, 3$$

$$\therefore \sum fx = f_1 x_1 + f_2 x_2 + f_3 x_3 + \dots + f_n x_n$$

$$\therefore \sum fx = 5 \times 3 + 15 \times 11 + 25 \times 7 + 35 \times 4 + 45 \times 10 + 55 \times 5 + 65 \times 7 + 75 \times 3 = 1900$$

$$\therefore \bar{X} = \frac{\sum fx}{\sum f} \quad \text{Here } \sum fx = 1900 \text{ \& } \sum f = 50$$

$$\therefore \bar{X} = \frac{1900}{50} = 38 \text{ cm. Ans.}$$

(ii) Short-cut method :- Formula is $\bar{X} = w + \frac{\sum f \cdot dx^2}{\sum f}$.

Where $\bar{X}$ - stands for mean.

w - stands for value of assumed mean.

$\sum f dx'$ - stands for summation of deviations obtained from assumed mean & multiplied by their frequencies.

$\sum f$ - stands for total number of observations.

Length of fish x	Frequency f	Deviation from assumed mean $dx' (45)$	Frequency deviation $f dx'$
5	3	$5 - 45 = -40$	-120
15	11	$15 - 45 = -30$	-330
25	7	$25 - 45 = -20$	-140
35	4	$35 - 45 = -10$	$-40 = -650$
45 (w)	10	$45 - 45 = 0$	0
55	5	$55 - 45 = +10$	+50
65	7	$65 - 45 = +20$	+140
75	3	$75 - 45 = +30$	+90 = 230
	$\Sigma f = 50$		$\Sigma f dx' = -400$

$$\therefore \bar{X} = w + \frac{\Sigma f dx'}{\Sigma f}, \text{ Here } N = 45, \Sigma f dx' = -400, \Sigma f = 50.$$

$$\therefore \bar{X} = 45 + \frac{-400}{50} = 45 + (-8) = 45 - 8 = 37 \text{ cms Ans.}$$

② Grouped data ③ Continuous Series - Mean is calculated in continuous series like discrete series with slight variation.

④ Direct Method: Mid value of each class interval is obtained by

$$\text{Mid value} = \frac{\text{Lower level of CI} + \text{Upper level of CI}}{2}$$

After obtaining ~~lower~~ mid value of each class interval continuous series is converted to discrete series & formula used as $\bar{X} = \frac{\Sigma f dx}{\Sigma f}$ (Direct method)

⑤ Short cut Method: - The same formula used in discrete series is applied by $\wedge$ width of class interval. $\bar{X} = w + \frac{\Sigma f dx'}{\Sigma f}$, i.e. where w = stands for assumed mean.

$\wedge$ = stands for width of class interval.

dx' = stands for deviation obtained from assumed Mean.

Σf = stands for total No. of observations.